## Q. 1 - Q. 5 carry one mark each.

Q. 1 Which of the following is CORRECT with respect to grammar and usage?

Mount Everest is $\qquad$ .
(A) the highest peak in the world
(B) highest peak in the world
(C) one of highest peak in the world
(D) one of the highest peak in the world
Q. 2 The policeman asked the victim of a theft, "What did you $\qquad$ ?"
(A) loose
(B) lose
(C) loss
(D) louse
Q. 3 Despite the new medicine's $\qquad$ in treating diabetes, it is not $\qquad$ widely.
(A) effectiveness --- prescribed
(B) availability --- used
(C) prescription --- available
(D) acceptance --- proscribed
Q. 4 In a huge pile of apples and oranges, both ripe and unripe mixed together, $15 \%$ are unripe fruits. Of the unripe fruits, $45 \%$ are apples. Of the ripe ones, $66 \%$ are oranges. If the pile contains a total of 5692000 fruits, how many of them are apples?
(A) 2029198
(B) 2467482
(C) 2789080
(D) 3577422
Q. 5 Michael lives 10 km away from where I live. Ahmed lives 5 km away and Susan lives 7 km away from where I live. Arun is farther away than Ahmed but closer than Susan from where I live. From the information provided here, what is one possible distance (in km ) at which I live from Arun's place?
(A) 3.00
(B) 4.99
(C) 6.02
(D) 7.01

## Q. 6 - Q. 10 carry two marks each.

Q. 6 A person moving through a tuberculosis prone zone has a $50 \%$ probability of becoming infected. However, only $30 \%$ of infected people develop the disease. What percentage of people moving through a tuberculosis prone zone remains infected but does not show symptoms of disease?
(A) 15
(B) 33
(C) 35
(D) 37
Q. 7 In a world filled with uncertainty, he was glad to have many good friends. He had always assisted them in times of need and was confident that they would reciprocate. However, the events of the last week proved him wrong.

Which of the following inference(s) is/are logically valid and can be inferred from the above passage?
(i) His friends were always asking him to help them.
(ii) He felt that when in need of help, his friends would let him down.
(iii) He was sure that his friends would help him when in need.
(iv) His friends did not help him last week.
(A) (i) and (ii)
(B) (iii) and (iv)
(C) (iii) only
(D) (iv) only
Q. 8 Leela is older than her cousin Pavithra. Pavithra's brother Shiva is older than Leela. When Pavithra and Shiva are visiting Leela, all three like to play chess. Pavithra wins more often than Leela does.

Which one of the following statements must be TRUE based on the above?
(A) When Shiva plays chess with Leela and Pavithra, he often loses.
(B) Leela is the oldest of the three.
(C) Shiva is a better chess player than Pavithra.
(D) Pavithra is the youngest of the three.
Q. 9 If $q^{-a}=\frac{1}{r}$ and $r^{-b}=\frac{1}{s}$ and $S^{-c}=\frac{1}{q}$, the value of $a b c$ is $\qquad$ $-$
(A) $(r q s)^{-1}$
(B) 0
(C) 1
(D) $r+q+s$
Q. $10 \mathbf{P}, \mathbf{Q}, \mathbf{R}$ and $\mathbf{S}$ are working on a project. $\mathbf{Q}$ can finish the task in 25 days, working alone for 12 hours a day. $\mathbf{R}$ can finish the task in 50 days, working alone for 12 hours per day. $\mathbf{Q}$ worked 12 hours a day but took sick leave in the beginning for two days. $\mathbf{R}$ worked 18 hours a day on all days. What is the ratio of work done by $\mathbf{Q}$ and $\mathbf{R}$ after 7 days from the start of the project?
(A) 10:11
(B) $11: 10$
(C) 20:21
(D) 21:20

## END OF THE QUESTION PAPER

## Q. 1 - Q. 25 carry one mark each.

Q. 1 Let $M^{4}=I$, (where $I$ denotes the identity matrix) and $M \neq I, M^{2} \neq I$ and $M^{3} \neq \mathrm{I}$. Then, for any natural number $k, \mathrm{M}^{-1}$ equals:
(A) $\mathrm{M}^{4 k+1}$
(B) $\mathrm{M}^{4 k+2}$
(C) $\mathrm{M}^{4 k+3}$
(D) $\mathrm{M}^{4 k}$
Q. 2 The second moment of a Poisson-distributed random variable is 2 . The mean of the random variable is $\qquad$
Q. 3 Given the following statements about a function $f: \mathbb{R} \rightarrow \mathbb{R}$, select the right option:

P : If $f(x)$ is continuous at $x=x_{0}$, then it is also differentiable at $x=x_{0}$.
Q: If $f(x)$ is continuous at $x=x_{0}$, then it may not be differentiable at $x=x_{0}$.
R: If $f(x)$ is differentiable at $x=x_{0}$, then it is also continuous at $x=x_{0}$.
(A) P is true, Q is false, R is false
(B) P is false, Q is true, R is true
(C) P is false, Q is true, R is false
(D) $P$ is true, Q is false, R is true
Q. 4 Which one of the following is a property of the solutions to the Laplace equation: $\nabla^{2} f=0$ ?
(A) The solutions have neither maxima nor minima anywhere except at the boundaries.
(B) The solutions are not separable in the coordinates.
(C) The solutions are not continuous.
(D) The solutions are not dependent on the boundary conditions.
Q. 5 Consider the plot of $f(x)$ versus $x$ as shown below.


Suppose $F(x)=\int_{-5}^{x} f(y) d y$. Which one of the following is a graph of $F(x)$ ?

(A)

(C)
(D)
(B)

Q. 6 Which one of the following is an eigen function of the class of all continuous-time, linear, timeinvariant systems ( $u(t)$ denotes the unit-step function)?
(A) $e^{j \omega_{0} t} u(t)$
(B) $\cos \left(\omega_{0} t\right)$
(C) $e^{j \omega_{0} t}$
(D) $\sin \left(\omega_{0} t\right)$
Q. $7 \quad$ A continuous-time function $x(t)$ is periodic with period $T$. The function is sampled uniformly with a sampling period $T_{s}$. In which one of the following cases is the sampled signal periodic?
(A) $T=\sqrt{2} T_{S}$
(B) $T=1.2 T_{s}$
(C) Always
(D) Never
Q. 8 Consider the sequence $x[n]=a^{n} u[n]+b^{n} u[n]$, where $u[n]$ denotes the unit-step sequence and $0<|a|<|b|<1$. The region of convergence (ROC) of the z-transform of $x[n]$ is
(A) $|z|>|a|$
(B) $|z|>|b|$
(C) $|z|<|a|$
(D) $|a|<|z|<|b|$
Q. 9 Consider a two-port network with the transmission matrix: $T=\left(\begin{array}{ll}A & B \\ C & D\end{array}\right)$. If the network is reciprocal, then
(A) $T^{-1}=T$
(B) $T^{2}=T$
(C) Determinant $(T)=0$
(D) Determinant $(T)=1$
Q. 10 A continuous-time sinusoid of frequency 33 Hz is multiplied with a periodic Dirac impulse train of frequency 46 Hz . The resulting signal is passed through an ideal analog low-pass filter with a cutoff frequency of 23 Hz . The fundamental frequency (in Hz ) of the output is $\qquad$
Q. 11 A small percentage of impurity is added to an intrinsic semiconductor at 300 K . Which one of the following statements is true for the energy band diagram shown in the following figure?

(A) Intrinsic semiconductor doped with pentavalent atoms to form $n$-type semiconductor
(B) Intrinsic semiconductor doped with trivalent atoms to form $n$-type semiconductor
(C) Intrinsic semiconductor doped with pentavalent atoms to form $p$-type semiconductor
(D) Intrinsic semiconductor doped with trivalent atoms to form $p$-type semiconductor
Q. 12 Consider the following statements for a metal oxide semiconductor field effect transistor (MOSFET):

P: As channel length reduces, OFF-state current increases.
Q: As channel length reduces, output resistance increases.
R: As channel length reduces, threshold voltage remains constant.
S: As channel length reduces, ON current increases.

Which of the above statements are INCORRECT?
(A) P and Q
(B) P and S
(C) Q and R
(D) R and S
Q. 13 Consider the constant current source shown in the figure below. Let $\beta$ represent the current gain of the transistor.


The load current $I_{0}$ through $R_{L}$ is
(A) $I_{0}=\left(\frac{\beta+1}{\beta}\right) \frac{V_{r e f}}{R}$
(B) $I_{0}=\left(\frac{\beta}{\beta+1}\right) \frac{V_{r e f}}{R}$
(C) $I_{0}=\left(\frac{\beta+1}{\beta}\right) \frac{V_{r e f}}{2 R}$
(D) $I_{0}=\left(\frac{\beta}{\beta+1}\right) \frac{V_{r e f}}{2 R}$
Q. 14 The following signal $V_{i}$ of peak voltage 8 V is applied to the non-inverting terminal of an ideal opamp. The transistor has $V_{B E}=0.7 \mathrm{~V}, \beta=100 ; V_{L E D}=1.5 \mathrm{~V}, V_{C C}=10 \mathrm{~V}$ and $-V_{C C}=-10 \mathrm{~V}$.


Vi


The number of times the LED glows is $\qquad$
Q. 15 Consider the oscillator circuit shown in the figure. The function of the network (shown in dotted lines) consisting of the $100 \mathrm{k} \Omega$ resistor in series with the two diodes connected back-to-back is to:

(A) introduce amplitude stabilization by preventing the op amp from saturating and thus producing sinusoidal oscillations of fixed amplitude
(B) introduce amplitude stabilization by forcing the opamp to swing between positive and negative saturation and thus producing square wave oscillations of fixed amplitude
(C) introduce frequency stabilization by forcing the circuit to oscillate at a single frequency
(D) enable the loop gain to take on a value that produces square wave oscillations
Q. 16 The block diagram of a frequency synthesizer consisting of a Phase Locked Loop (PLL) and a divide-by- $N$ counter (comprising $\div 2, \div 4, \div 8, \div 16$ outputs) is sketched below. The synthesizer is excited with a 5 kHz signal (Input 1). The free-running frequency of the PLL is set to 20 kHz . Assume that the commutator switch makes contacts repeatedly in the order 1-2-3-4.


The corresponding frequencies synthesized are:
(A) $10 \mathrm{kHz}, 20 \mathrm{kHz}, 40 \mathrm{kHz}, 80 \mathrm{kHz}$
(B) $20 \mathrm{kHz}, 40 \mathrm{kHz}, 80 \mathrm{kHz}, 160 \mathrm{kHz}$
(C) $80 \mathrm{kHz}, 40 \mathrm{kHz}, 20 \mathrm{kHz}, 10 \mathrm{kHz}$
(D) $160 \mathrm{kHz}, 80 \mathrm{kHz}, 40 \mathrm{kHz}, 20 \mathrm{kHz}$
Q. 17 The output of the combinational circuit given below is

(A) $\mathrm{A}+\mathrm{B}+\mathrm{C}$
(B) $\mathrm{A}(\mathrm{B}+\mathrm{C})$
(C) $\mathrm{B}(\mathrm{C}+\mathrm{A})$
(D) $\mathrm{C}(\mathrm{A}+\mathrm{B})$
Q. 18 What is the voltage $V_{\text {out }}$ in the following circuit?

(A) 0 V
(B) $\left(\mid \mathrm{V}_{\mathrm{T}}\right.$ of PMOS $\mid+\mathrm{V}_{\mathrm{T}}$ of NMOS) $/ 2$
(C) Switching threshold of inverter
(D) $V_{D D}$
Q. 19 Match the inferences X, Y, and Z, about a system, to the corresponding properties of the elements of first column in Routh's Table of the system characteristic equation.

X : The system is stable ...
Y: The system is unstable ...
Z: The test breaks down ...
(A) $\mathrm{X} \rightarrow \mathrm{P}, \mathrm{Y} \rightarrow \mathrm{Q}, \mathrm{Z} \rightarrow \mathrm{R}$
(B) $\mathrm{X} \rightarrow \mathrm{Q}, \mathrm{Y} \rightarrow \mathrm{P}, \mathrm{Z} \rightarrow \mathrm{R}$
(C) $\mathrm{X} \rightarrow \mathrm{R}, \mathrm{Y} \rightarrow \mathrm{Q}, \mathrm{Z} \rightarrow \mathrm{P}$
(D) $\mathrm{X} \rightarrow \mathrm{P}, \mathrm{Y} \rightarrow \mathrm{R}, \mathrm{Z} \rightarrow \mathrm{Q}$
Q. 20 A closed-loop control system is stable if the Nyquist plot of the corresponding open-loop transfer function
(A) encircles the $s$-plane point $(-1+j 0)$ in the counterclockwise direction as many times as the number of right-half $s$-plane poles.
(B) encircles the $s$-plane point $(0-j 1)$ in the clockwise direction as many times as the number of right-half $s$-plane poles.
(C) encircles the $s$-plane point $(-1+j 0)$ in the counterclockwise direction as many times as the number of left-half $s$-plane poles.
(D) encircles the $s$-plane point $(-1+j 0)$ in the counterclockwise direction as many times as the number of right-half $s$-plane zeros.
Q. 21 Consider binary data transmission at a rate of 56 kbps using baseband binary pulse amplitude modulation (PAM) that is designed to have a raised-cosine spectrum. The transmission bandwidth (in kHz ) required for a roll-off factor of 0.25 is $\qquad$
Q. 22 A superheterodyne receiver operates in the frequency range of $58 \mathrm{MHz}-68 \mathrm{MHz}$. The intermediate frequency $f_{I F}$ and local oscillator frequency $f_{L O}$ are chosen such that $f_{I F} \leq f_{L O}$. It is required that the image frequencies fall outside the $58 \mathrm{MHz}-68 \mathrm{MHz}$ band. The minimum required $f_{I F}$ (in MHz) is $\qquad$
Q. 23 The amplitude of a sinusoidal carrier is modulated by a single sinusoid to obtain the amplitude modulated signal $s(t)=5 \cos 1600 \pi t+20 \cos 1800 \pi t+5 \cos 2000 \pi t$. The value of the modulation index is $\qquad$
Q. 24 Concentric spherical shells of radii $2 \mathrm{~m}, 4 \mathrm{~m}$, and 8 m carry uniform surface charge densities of $20 \mathrm{nC} / \mathrm{m}^{2},-4 \mathrm{nC} / \mathrm{m}^{2}$ and $\rho_{\mathrm{s}}$, respectively. The value of $\rho_{\mathrm{s}}\left(\mathrm{nC} / \mathrm{m}^{2}\right)$ required to ensure that the electric flux density $\vec{D}=\overrightarrow{0}$ at radius 10 m is $\qquad$
Q. 25 The propagation constant of a lossy transmission line is $(2+j 5) \mathrm{m}^{-1}$ and its characteristic impedance is $(50+j 0) \Omega$ at $\omega=10^{6} \mathrm{rad} \mathrm{s}^{-1}$. The values of the line constants $\mathrm{L}, \mathrm{C}, \mathrm{R}, \mathrm{G}$ are, respectively,
(A) $\mathrm{L}=200 \mu \mathrm{H} / \mathrm{m}, \mathrm{C}=0.1 \mu \mathrm{~F} / \mathrm{m}, \mathrm{R}=50 \Omega / \mathrm{m}, \mathrm{G}=0.02 \mathrm{~S} / \mathrm{m}$
(B) $\mathrm{L}=250 \mu \mathrm{H} / \mathrm{m}, \mathrm{C}=0.1 \mu \mathrm{~F} / \mathrm{m}, \mathrm{R}=100 \Omega / \mathrm{m}, \mathrm{G}=0.04 \mathrm{~S} / \mathrm{m}$
(C) $\mathrm{L}=200 \mu \mathrm{H} / \mathrm{m}, \mathrm{C}=0.2 \mu \mathrm{~F} / \mathrm{m}, \mathrm{R}=100 \Omega / \mathrm{m}, \mathrm{G}=0.02 \mathrm{~S} / \mathrm{m}$
(D) $\mathrm{L}=250 \mu \mathrm{H} / \mathrm{m}, \mathrm{C}=0.2 \mu \mathrm{~F} / \mathrm{m}, \mathrm{R}=50 \Omega / \mathrm{m}, \mathrm{G}=0.04 \mathrm{~S} / \mathrm{m}$

## Q. 26 - Q. 55 carry two marks each.

Q. 26 The integral $\frac{1}{2 \pi} \iint_{D}(x+y+10) d x d y$, where $D$ denotes the disc: $x^{2}+y^{2} \leq 4$, evaluates to $\qquad$
Q. 27 A sequence $x[n]$ is specified as
$\left[\begin{array}{c}x[n] \\ x[n-1]\end{array}\right]=\left[\begin{array}{ll}1 & 1 \\ 1 & 0\end{array}\right]^{n}\left[\begin{array}{l}1 \\ 0\end{array}\right]$, for $n \geq 2$.
The initial conditions are $x[0]=1, x[1]=1$, and $x[n]=0$ for $n<0$. The value of $x[12]$ is $\qquad$
Q. 28 In the following integral, the contour $C$ encloses the points $2 \pi j$ and $-2 \pi j$

$$
-\frac{1}{2 \pi} \oint_{C} \frac{\sin z}{(z-2 \pi j)^{3}} d z
$$

The value of the integral is $\qquad$
Q. 29 The region specified by $\left\{(\rho, \varphi, z): 3 \leq \rho \leq 5, \frac{\pi}{8} \leq \varphi \leq \frac{\pi}{4}, 3 \leq \mathrm{z} \leq 4.5\right\}$ in cylindrical coordinates has volume of $\qquad$
Q. 30 The Laplace transform of the causal periodic square wave of period $T$ shown in the figure below is

(A) $F(s)=\frac{1}{1+e^{-s T / 2}}$
(B) $F(s)=\frac{1}{s\left(1+e^{-\frac{s T}{2}}\right)}$
(C) $F(s)=\frac{1}{s\left(1-e^{-s T}\right)}$
(D) $F(s)=\frac{1}{1-e^{-s T}}$
Q. 31 A network consisting of a finite number of linear resistor (R), inductor (L), and capacitor (C) elements, connected all in series or all in parallel, is excited with a source of the form

$$
\sum_{k=1}^{3} a_{k} \cos \left(k \omega_{0} t\right), \text { where } a_{k} \neq 0, \omega_{0} \neq 0
$$

The source has nonzero impedance. Which one of the following is a possible form of the output measured across a resistor in the network?
(A)
$\sum_{k=1}^{3} b_{k} \cos \left(k \omega_{0} t+\phi_{k}\right)$, where $b_{k} \neq a_{k}, \forall k$
(B)
$\sum_{k=1}^{4} b_{k} \cos \left(k \omega_{0} t+\phi_{k}\right)$, where $b_{k} \neq 0, \forall k$
(C)

$$
\sum_{k=1}^{3} a_{k} \cos \left(k \omega_{0} t+\phi_{k}\right)
$$

(D)

$$
\sum_{k=1}^{2} a_{k} \cos \left(k \omega_{0} t+\phi_{k}\right)
$$

Q. 32 A first-order low-pass filter of time constant $T$ is excited with different input signals (with zero initial conditions up to $t=0$ ). Match the excitation signals $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ with the corresponding time responses for $t \geq 0$ :

X : Impulse
Y: Unit step
Z: Ramp
(A) $\mathrm{X} \rightarrow \mathrm{R}, \mathrm{Y} \rightarrow \mathrm{Q}, \mathrm{Z} \rightarrow \mathrm{P}$
(B) $\mathrm{X} \rightarrow \mathrm{Q}, \mathrm{Y} \rightarrow \mathrm{P}, \mathrm{Z} \rightarrow \mathrm{R}$
(C) $\mathrm{X} \rightarrow \mathrm{R}, \mathrm{Y} \rightarrow \mathrm{P}, \mathrm{Z} \rightarrow \mathrm{Q}$
(D) $\mathrm{X} \rightarrow \mathrm{P}, \mathrm{Y} \rightarrow \mathrm{R}, \mathrm{Z} \rightarrow \mathrm{Q}$
Q. 33 An AC voltage source $V=10 \sin (t)$ volts is applied to the following network. Assume that $R_{1}=3$ $\mathrm{k} \Omega, R_{2}=6 \mathrm{k} \Omega$ and $R_{3}=9 \mathrm{k} \Omega$, and that the diode is ideal.


RMS current $\mathrm{I}_{r m s}$ (in mA ) through the diode is $\qquad$
Q. 34 In the circuit shown in the figure, the maximum power (in watt) delivered to the resistor $R$ is $\qquad$

Q. 35 Consider the signal

$$
x[n]=6 \delta[n+2]+3 \delta[n+1]+8 \delta[n]+7 \delta[n-1]+4 \delta[n-2] .
$$

If $X\left(e^{j \omega}\right)$ is the discrete-time Fourier transform of $x[n]$, then $\frac{1}{\pi} \int_{-\pi}^{\pi} X\left(e^{j \omega}\right) \sin ^{2}(2 \omega) d \omega$ is equal to $\qquad$
Q. 36 Consider a silicon p-n junction with a uniform acceptor doping concentration of $10^{17} \mathrm{~cm}^{-3}$ on the pside and a uniform donor doping concentration of $10^{16} \mathrm{~cm}^{-3}$ on the n -side. No external voltage is applied to the diode. Given: $k T / q=26 \mathrm{mV}, n_{i}=1.5 \times 10^{10} \mathrm{~cm}^{-3}, \varepsilon_{\mathrm{Si}}=12 \varepsilon_{0}, \varepsilon_{0}=8.85 \times 10^{-14} \mathrm{~F} / \mathrm{m}$, and $q=1.6 \times 10^{-19} \mathrm{C}$.
The charge per unit junction area ( $\mathrm{nC} \mathrm{cm}^{-2}$ ) in the depletion region on the p -side is $\qquad$
Q. 37 Consider an $n$-channel metal oxide semiconductor field effect transistor (MOSFET) with a gate-tosource voltage of 1.8 V . Assume that $\frac{W}{L}=4, \mu_{N} C_{o x}=70 \times 10^{-6} \mathrm{AV}^{-2}$, the threshold voltage is 0.3 V , and the channel length modulation parameter is $0.09 \mathrm{~V}^{-1}$. In the saturation region, the drain conductance (in micro seimens) is $\qquad$
Q. 38 The figure below shows the doping distribution in a $p$-type semiconductor in $\log$ scale.


The magnitude of the electric field (in $\mathrm{kV} / \mathrm{cm}$ ) in the semiconductor due to non uniform doping is $\qquad$
Q. 39 Consider a silicon sample at $\mathrm{T}=300 \mathrm{~K}$, with a uniform donor density $N_{d}=5 \times 10^{16} \mathrm{~cm}^{-3}$, illuminated uniformly such that the optical generation rate is $G_{\text {opt }}=1.5 \times 10^{20} \mathrm{~cm}^{-3} \mathrm{~s}^{-1}$ throughout the sample. The incident radiation is turned off at $t=0$. Assume low-level injection to be valid and ignore surface effects. The carrier lifetimes are $\tau_{p 0}=0.1 \mu \mathrm{~s}$ and $\tau_{n 0}=0.5 \mu \mathrm{~s}$.


The hole concentration at $t=0$ and the hole concentration at $t=0.3 \mu \mathrm{~s}$, respectively, are
(A) $1.5 \times 10^{13} \mathrm{~cm}^{-3}$ and $7.47 \times 10^{11} \mathrm{~cm}^{-3}$
(B) $1.5 \times 10^{13} \mathrm{~cm}^{-3}$ and $8.23 \times 10^{11} \mathrm{~cm}^{-3}$
(C) $7.5 \times 10^{13} \mathrm{~cm}^{-3}$ and $3.73 \times 10^{11} \mathrm{~cm}^{-3}$
(D) $7.5 \times 10^{13} \mathrm{~cm}^{-3}$ and $4.12 \times 10^{11} \mathrm{~cm}^{-3}$
Q. 40 An ideal opamp has voltage sources $\mathrm{V}_{1}, \mathrm{~V}_{3}, \mathrm{~V}_{5}, \ldots, \mathrm{~V}_{\mathrm{N}-1}$ connected to the non-inverting input and $\mathrm{V}_{2}$, $\mathrm{V}_{4}, \mathrm{~V}_{6}, \ldots, \mathrm{~V}_{\mathrm{N}}$ connected to the inverting input as shown in the figure below $\left(+\mathrm{V}_{\mathrm{CC}}=15\right.$ volt, $-\mathrm{V}_{\mathrm{CC}}=-15$ volt). The voltages $\mathrm{V}_{1}, \mathrm{~V}_{2}, \mathrm{~V}_{3}, \mathrm{~V}_{4}, \mathrm{~V}_{5}, \mathrm{~V}_{6}, \ldots$ are $1,-1 / 2,1 / 3,-1 / 4,1 / 5,-1 / 6, \ldots$ volt, respectively. As N approaches infinity, the output voltage (in volt) is $\qquad$

Q. 41 A p-i-n photodiode of responsivity $0.8 \mathrm{~A} / \mathrm{W}$ is connected to the inverting input of an ideal opamp as shown in the figure, $+\mathrm{Vcc}=15 \mathrm{~V},-\mathrm{Vcc}=-15 \mathrm{~V}$, Load resistor $R_{L}=10 \mathrm{k} \Omega$. If $10 \mu \mathrm{~W}$ of power is incident on the photodiode, then the value of the photocurrent (in $\mu \mathrm{A}$ ) through the load is $\qquad$

Q. 42 Identify the circuit below.

(A) Binary to Gray code converter
(B) Binary to XS3 converter
(C) Gray to Binary converter
(D) XS3 to Binary converter
Q. 43 The functionality implemented by the circuit below is


- is a tristate buffer
(A) 2-to-1 multiplexer
(B) 4-to-1 multiplexer
(C) 7-to-1 multiplexer
(D) 6-to-1 multiplexer
Q. 44 In an 8085 system, a PUSH operation requires more clock cycles than a POP operation. Which one of the following options is the correct reason for this?
(A) For POP, the data transceivers remain in the same direction as for instruction fetch (memory to processor), whereas for PUSH their direction has to be reversed.
(B) Memory write operations are slower than memory read operations in an 8085 based system.
(C) The stack pointer needs to be pre-decremented before writing registers in a PUSH, whereas a POP operation uses the address already in the stack pointer.
(D) Order of registers has to be interchanged for a PUSH operation, whereas POP uses their natural order.
Q. 45 The open-loop transfer function of a unity-feedback control system is

$$
G(s)=\frac{K}{s^{2}+5 s+5}
$$

The value of $K$ at the breakaway point of the feedback control system's root-locus plot is $\qquad$
Q. 46 The open-loop transfer function of a unity-feedback control system is given by

$$
G(s)=\frac{K}{s(s+2)}
$$

For the peak overshoot of the closed-loop system to a unit step input to be $10 \%$, the value of K is
Q. 47 The transfer function of a linear time invariant system is given by
$\mathrm{H}(\mathrm{s})=2 s^{4}-5 s^{3}+5 s-2$
The number of zeros in the right half of the s-plane is $\qquad$
Q. 48 Consider a discrete memoryless source with alphabet $S=\left\{s_{0}, s_{1}, s_{2}, s_{3}, s_{4}, \ldots\right\}$ and respective probabilities of occurrence $P=\left\{\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}, \frac{1}{32}, \ldots\right\}$. The entropy of the source (in bits) is $\qquad$
Q. 49 A digital communication system uses a repetition code for channel encoding/decoding. During transmission, each bit is repeated three times ( 0 is transmitted as 000 , and 1 is transmitted as 111). It is assumed that the source puts out symbols independently and with equal probability. The decoder operates as follows: In a block of three received bits, if the number of zeros exceeds the number of ones, the decoder decides in favor of a 0 , and if the number of ones exceeds the number of zeros, the decoder decides in favor of a 1 . Assuming a binary symmetric channel with crossover probability $\mathrm{p}=0.1$, the average probability of error is $\qquad$
Q. 50 An analog pulse $s(t)$ is transmitted over an additive white Gaussian noise (AWGN) channel. The received signal is $r(t)=s(t)+n(t)$, where $n(t)$ is additive white Gaussian noise with power spectral density $\frac{N_{0}}{2}$. The received signal is passed through a filter with impulse response $h(t)$. Let $E_{s}$ and $E_{h}$ denote the energies of the pulse $s(t)$ and the filter $h(t)$, respectively. When the signal-to-noise ratio (SNR) is maximized at the output of the filter $\left(\mathrm{SNR}_{\text {max }}\right)$, which of the following holds?
(A) $E_{s}=E_{h} ; \mathrm{SNR}_{\text {max }}=\frac{2 E_{s}}{N_{0}}$
(B) $E_{s}=E_{h} ; \mathrm{SNR}_{\text {max }}=\frac{E_{s}}{2 N_{0}}$
(C) $E_{s}>E_{h} ; \mathrm{SNR}_{\text {max }}>\frac{2 E_{s}}{N_{0}}$
(D) $E_{S}<E_{h} ; \mathrm{SNR}_{\text {max }}=\frac{2 E_{h}}{N_{0}}$
Q. 51 The current density in a medium is given by

$$
\vec{J}=\frac{400 \sin \theta}{2 \pi\left(r^{2}+4\right)} \hat{a}_{r} \mathrm{Am}^{-2}
$$

The total current and the average current density flowing through the portion of a spherical surface $r=0.8 \mathrm{~m}, \frac{\pi}{12} \leq \theta \leq \frac{\pi}{4}, 0 \leq \phi \leq 2 \pi$ are given, respectively, by
(A) $15.09 \mathrm{~A}, 12.86 \mathrm{Am}^{-2}$
(B) $18.73 \mathrm{~A}, 13.65 \mathrm{Am}^{-2}$
(C) $12.86 \mathrm{~A}, 9.23 \mathrm{Am}^{-2}$
(D) $10.28 \mathrm{~A}, 7.56 \mathrm{Am}^{-2}$
Q. 52 An antenna pointing in a certain direction has a noise temperature of 50 K . The ambient temperature is 290 K . The antenna is connected to a pre-amplifier that has a noise figure of 2 dB and an available gain of 40 dB over an effective bandwidth of 12 MHz . The effective input noise temperature $T_{e}$ for the amplifier and the noise power $\mathrm{P}_{\mathrm{a} \text { o }}$ at the output of the preamplifier, respectively, are
(A) $\mathrm{T}_{\mathrm{e}}=169.36 \mathrm{~K}$ and $\mathrm{P}_{\mathrm{ao}}=3.73 \times 10^{-10} \mathrm{~W}$
(B) $\mathrm{T}_{\mathrm{e}}=170.8 \mathrm{~K}$ and $\mathrm{P}_{\text {ao }}=4.56 \times 10^{-10} \mathrm{~W}$
(C) $\mathrm{T}_{\mathrm{e}}=182.5 \mathrm{~K}$ and $\mathrm{P}_{\text {ao }}=3.85 \times 10^{-10} \mathrm{~W}$
(D) $\mathrm{T}_{\mathrm{e}}=160.62 \mathrm{~K}$ and $\mathrm{P}_{\text {ao }}=4.6 \times 10^{-10} \mathrm{~W}$
Q. 53 Two lossless X-band horn antennas are separated by a distance of 200 . The amplitude reflection coefficients at the terminals of the transmitting and receiving antennas are 0.15 and 0.18 , respectively. The maximum directivities of the transmitting and receiving antennas (over the isotropic antenna) are 18 dB and 22 dB , respectively. Assuming that the input power in the lossless transmission line connected to the antenna is 2 W , and that the antennas are perfectly aligned and polarization matched, the power ( in mW ) delivered to the load at the receiver is $\qquad$
Q. 54 The electric field of a uniform plane wave travelling along the negative $z$ direction is given by the following equation:

$$
\vec{E}_{w}^{i}=\left(\hat{a}_{x}+j \hat{a}_{y}\right) E_{0} e^{j k z}
$$

This wave is incident upon a receiving antenna placed at the origin and whose radiated electric field towards the incident wave is given by the following equation:

$$
\vec{E}_{a}=\left(\hat{a}_{x}+2 \hat{a}_{y}\right) E_{I} \frac{1}{r} e^{-j k r}
$$

The polarization of the incident wave, the polarization of the antenna and losses due to the polarization mismatch are, respectively,
(A) Linear, Circular (clockwise), -5 dB
(B) Circular (clockwise), Linear, -5 dB
(C) Circular (clockwise), Linear, -3dB
(D) Circular (anti clockwise), Linear, -3dB
Q. 55 The far-zone power density radiated by a helical antenna is approximated as:

$$
\vec{W}_{\text {rad }}=\vec{W}_{\text {average }} \approx \widehat{a_{r}} C_{0} \frac{1}{r^{2}} \cos ^{4} \theta
$$

The radiated power density is symmetrical with respect to $\phi$ and exists only in the upper hemisphere: $0 \leq \theta \leq \frac{\pi}{2} ; 0 \leq \phi \leq 2 \pi ; C_{0}$ is a constant. The power radiated by the antenna (in watts) and the maximum directivity of the antenna, respectively, are
(A) $1.5 \mathrm{C}_{0}, 10 \mathrm{~dB}$
(B) $1.256 \mathrm{C}_{0}, 10 \mathrm{~dB}$
(C) $1.256 \mathrm{C}_{0}, 12 \mathrm{~dB}$
(D) $1.5 \mathrm{C}_{0}, 12 \mathrm{~dB}$

## END OF THE QUESTION PAPER

## Q. 1 - Q. 5 carry one mark each.

Q. 1 Based on the given statements, select the appropriate option with respect to grammar and usage.

Statements
(i) The height of Mr. $\mathbf{X}$ is 6 feet.
(ii) The height of Mr. $\mathbf{Y}$ is 5 feet.
(A) Mr. $\mathbf{X}$ is longer than $\mathrm{Mr} . \mathbf{Y}$.
(B) Mr. $\mathbf{X}$ is more elongated than $\mathrm{Mr} . \mathbf{Y}$.
(C) Mr. $\mathbf{X}$ is taller than $\mathbf{M r} \mathbf{Y}$.
(D) Mr. $\mathbf{X}$ is lengthier than Mr. $\mathbf{Y}$.
Q. 2 The students $\qquad$ the teacher on teachers' day for twenty years of dedicated teaching.
(A) facilitated
(B) felicitated
(C) fantasized
(D) facillitated
Q. 3 After India's cricket world cup victory in 1985, Shrotria who was playing both tennis and cricket till then, decided to concentrate only on cricket. And the rest is history.

What does the underlined phrase mean in this context?
(A) history will rest in peace
(B) rest is recorded in history books
(C) rest is well known
(D) rest is archaic
Q. 4 Given $(9 \text { inches })^{1 / 2}=(0.25 \text { yards })^{1 / 2}$, which one of the following statements is TRUE?
(A) 3 inches $=0.5$ yards
(B) 9 inches $=1.5$ yards
(C) 9 inches $=0.25$ yards
(D) 81 inches $=0.0625$ yards
Q. $5 \quad \boldsymbol{S}, \boldsymbol{M}, \boldsymbol{E}$ and $\boldsymbol{F}$ are working in shifts in a team to finish a project. $\boldsymbol{M}$ works with twice the efficiency of others but for half as many days as $\boldsymbol{E}$ worked. $\boldsymbol{S}$ and $\boldsymbol{M}$ have 6 hour shifts in a day, whereas $\boldsymbol{E}$ and $\boldsymbol{F}$ have 12 hours shifts. What is the ratio of contribution of $\boldsymbol{M}$ to contribution of $\boldsymbol{E}$ in the project?
(A) 1:1
(B) $1: 2$
(C) $1: 4$
(D) 2:1

## Q. 6 - Q. 10 carry two marks each.

Q. 6 The Venn diagram shows the preference of the student population for leisure activities.


From the data given, the number of students who like to read books or play sports is $\qquad$ .
(A) 44
(B) 51
(C) 79
(D) 108
Q. 7 Social science disciplines were in existence in an amorphous form until the colonial period when they were institutionalized. In varying degrees, they were intended to further the colonial interest. In the time of globalization and the economic rise of postcolonial countries like India, conventional ways of knowledge production have become obsolete.

Which of the following can be logically inferred from the above statements?
(i) Social science disciplines have become obsolete.
(ii) Social science disciplines had a pre-colonial origin.
(iii) Social science disciplines always promote colonialism.
(iv) Social science must maintain disciplinary boundaries.
(A) (ii) only
(B) (i) and (iii) only
(C) (ii) and (iv) only
(D) (iii) and (iv) only
Q. 8 Two and a quarter hours back, when seen in a mirror, the reflection of a wall clock without number markings seemed to show $1: 30$. What is the actual current time shown by the clock?
(A) $8: 15$
(B) $11: 15$
(C) $12: 15$
(D) 12:45
Q. $9 \quad \mathbf{M}$ and $\mathbf{N}$ start from the same location. M travels 10 km East and then 10 km North-East. $\mathbf{N}$ travels 5 km South and then 4 km South-East. What is the shortest distance (in km ) between $\mathbf{M}$ and $\mathbf{N}$ at the end of their travel?
(A) 18.60
(B) 22.50
(C) 20.61
(D) 25.00
Q. 10 A wire of length 340 mm is to be cut into two parts. One of the parts is to be made into a square and the other into a rectangle where sides are in the ratio of $1: 2$. What is the length of the side of the square (in mm ) such that the combined area of the square and the rectangle is a MINIMUM?
(A) 30
(B) 40
(C) 120
(D) 180

## END OF THE QUESTION PAPER

## Q. 1 - Q. 25 carry one mark each.

Q. 1

The value of $x$ for which the matrix $A=\left[\begin{array}{ccc}3 & 2 & 4 \\ 9 & 7 & 13 \\ -6 & -4 & -9+x\end{array}\right]$ has zero as an eigenvalue is $\qquad$
Q. 2 Consider the complex valued function $f(z)=2 z^{3}+b|z|^{3}$ where $z$ is a complex variable. The value of $b$ for which the function $f(z)$ is analytic is $\qquad$
Q. 3 As $x$ varies from -1 to +3 , which one of the following describes the behaviour of the function $f(x)=x^{3}-3 x^{2}+1$ ?
(A) $f(x)$ increases monotonically.
(B) $f(x)$ increases, then decreases and increases again.
(C) $f(x)$ decreases, then increases and decreases again.
(D) $f(x)$ increases and then decreases.
Q. 4 How many distinct values of $x$ satisfy the equation $\sin (x)=x / 2$, where $x$ is in radians?
(A) 1
(B) 2
(C) 3
(D) 4 or more
Q. 5 Consider the time-varying vector $\mathbf{I}=\widehat{\mathbf{x}} 15 \cos (\omega t)+\hat{\mathbf{y}} 5 \sin (\omega t)$ in Cartesian coordinates, where $\omega>0$ is a constant. When the vector magnitude $|\mathbf{I}|$ is at its minimum value, the angle $\theta$ that $\mathbf{I}$ makes with the $x$ axis (in degrees, such that $0 \leq \theta \leq 180$ ) is $\qquad$
Q. 6 In the circuit shown below, $V_{S}$ is a constant voltage source and $I_{L}$ is a constant current load.


The value of $I_{L}$ that maximizes the power absorbed by the constant current load is
(A) $\frac{V_{S}}{4 R}$
(B) $\frac{V_{S}}{2 R}$
(C) $\frac{V_{S}}{R}$
(D) $\infty$
Q. 7 The switch has been in position 1 for a long time and abruptly changes to position 2 at $t=0$.


If time $t$ is in seconds, the capacitor voltage $\mathrm{V}_{\mathrm{C}}$ (in volts) for $t>0$ is given by
(A) $4(1-\exp (-t / 0.5))$
(B) $10-6 \exp (-t / 0.5)$
(C) $4(1-\exp (-t / 0.6))$
(D) $10-6 \exp (-t / 0.6)$
Q. 8 The figure shows an RLC circuit with a sinusoidal current source.


At resonance, the ratio $\left|\mathbf{I}_{\mathbf{L}}\right| / / \mathbf{I}_{\mathbf{R}} \mid$, i.e., the ratio of the magnitudes of the inductor current phasor and the resistor current phasor, is $\qquad$
Q. 9 The z-parameter matrix for the two-port network shown is

$$
\left[\begin{array}{cc}
2 j \omega & j \omega \\
j \omega & 3+2 j \omega
\end{array}\right]
$$

where the entries are in $\Omega$. Suppose $Z_{b}(j \omega)=R_{b}+j \omega$.


Then the value of $R_{b}$ (in $\Omega$ ) equals $\qquad$
Q. 10 The energy of the signal $x(t)=\frac{\sin (4 \pi t)}{4 \pi t}$ is $\qquad$
Q. 11 The Ebers-Moll model of a BJT is valid
(A) only in active mode
(B) only in active and saturation modes
(C) only in active and cut-off modes
(D) in active, saturation and cut-off modes
Q. 12 A long-channel NMOS transistor is biased in the linear region with $V_{D S}=50 \mathrm{mV}$ and is used as a resistance. Which one of the following statements is NOT correct?
(A) If the device width $W$ is increased, the resistance decreases.
(B) If the threshold voltage is reduced, the resistance decreases.
(C) If the device length $L$ is increased, the resistance increases.
(D) If $V_{G S}$ is increased, the resistance increases.
Q. 13 Assume that the diode in the figure has $V_{o n}=0.7 \mathrm{~V}$, but is otherwise ideal.


The magnitude of the current $\mathrm{i}_{2}$ (in mA ) is equal to $\qquad$
Q. 14 Resistor $R_{1}$ in the circuit below has been adjusted so that $I_{1}=1 \mathrm{~mA}$. The bipolar transistors Q1 and Q2 are perfectly matched and have very high current gain, so their base currents are negligible. The supply voltage $\mathrm{V}_{\mathrm{cc}}$ is 6 V . The thermal voltage $k T / q$ is 26 mV .


The value of $R_{2}$ (in $\Omega$ ) for which $I_{2}=100 \mu \mathrm{~A}$ is $\qquad$
Q. 15 Which one of the following statements is correct about an ac-coupled common-emitter amplifier operating in the mid-band region?
(A) The device parasitic capacitances behave like open circuits, whereas coupling and bypass capacitances behave like short circuits.
(B) The device parasitic capacitances, coupling capacitances and bypass capacitances behave like open circuits.
(C) The device parasitic capacitances, coupling capacitances and bypass capacitances behave like short circuits.
(D) The device parasitic capacitances behave like short circuits, whereas coupling and bypass capacitances behave like open circuits.
Q. 16 Transistor geometries in a CMOS inverter have been adjusted to meet the requirement for worst case charge and discharge times for driving a load capacitor C. This design is to be converted to that of a NOR circuit in the same technology, so that its worst case charge and discharge times while driving the same capacitor are similar. The channel lengths of all transistors are to be kept unchanged. Which one of the following statements is correct?

(A) Widths of PMOS transistors should be doubled, while widths of NMOS transistors should be halved.
(B) Widths of PMOS transistors should be doubled, while widths of NMOS transistors should not be changed.
(C) Widths of PMOS transistors should be halved, while widths of NMOS transistors should not be changed.
(D) Widths of PMOS transistors should be unchanged, while widths of NMOS transistors should be halved.
Q. 17 Assume that all the digital gates in the circuit shown in the figure are ideal, the resistor $R=10 \mathrm{k} \Omega$ and the supply voltage is 5 V . The D flip-flops $\mathrm{D}_{1}, \mathrm{D}_{2}, \mathrm{D}_{3}, \mathrm{D}_{4}$ and $\mathrm{D}_{5}$ are initialized with logic values $0,1,0,1$ and 0 , respectively. The clock has a $30 \%$ duty cycle.


The average power dissipated (in mW ) in the resistor $R$ is $\qquad$
Q.18 A 4:1 multiplexer is to be used for generating the output carry of a full adder. A and B are the bits to be added while $C_{\text {in }}$ is the input carry and $C_{\text {out }}$ is the output carry. A and B are to be used as the select bits with A being the more significant select bit.


Which one of the following statements correctly describes the choice of signals to be connected to the inputs $\mathrm{I}_{0}, \mathrm{I}_{1}, \mathrm{I}_{2}$ and $\mathrm{I}_{3}$ so that the output is $\mathrm{C}_{\text {out }}$ ?
(A) $\mathrm{I}_{0}=0, \mathrm{I}_{1}=\mathrm{C}_{\text {in }}, \mathrm{I}_{2}=\mathrm{C}_{\text {in }}$ and $\mathrm{I}_{3}=1$
(B) $\mathrm{I}_{0}=1, \mathrm{I}_{1}=\mathrm{C}_{\text {in }}, \mathrm{I}_{2}=\mathrm{C}_{\text {in }}$ and $\mathrm{I}_{3}=1$
(C) $\mathrm{I}_{0}=\mathrm{C}_{\text {in }}, \mathrm{I}_{1}=0, \mathrm{I}_{2}=1$ and $\mathrm{I}_{3}=\mathrm{C}_{\text {in }}$
(D) $\mathrm{I}_{0}=0, \mathrm{I}_{1}=\mathrm{C}_{\text {in }}, \mathrm{I}_{2}=1$ and $\mathrm{I}_{3}=\mathrm{C}_{\text {in }}$
Q. 19 The response of the system $G(s)=\frac{s-2}{(s+1)(s+3)}$ to the unit step input $u(t)$ is $y(t)$.

The value of $\frac{d y}{d t}$ at $t=0^{+}$is $\qquad$
Q. 20 The number and direction of encirclements around the point $-1+j 0$ in the complex plane by the Nyquist plot of $G(S)=\frac{1-s}{4+2 s}$ is
(A) zero.
(B) one, anti-clockwise.
(C) one, clockwise.
(D) two, clockwise.
Q. 21 A discrete memoryless source has an alphabet $\left\{a_{1}, a_{2}, a_{3}, a_{4}\right\}$ with corresponding probabilities $\left\{\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{8}\right\}$. The minimum required average codeword length in bits to represent this source for error-free reconstruction is $\qquad$
Q. 22 A speech signal is sampled at 8 kHz and encoded into PCM format using 8 bits/sample. The PCM data is transmitted through a baseband channel via 4-level PAM. The minimum bandwidth (in kHz ) required for transmission is $\qquad$
Q. 23 A uniform and constant magnetic field $\mathbf{B}=\hat{\mathbf{z}} B$ exists in the $\hat{\mathbf{z}}$ direction in vacuum. A particle of mass $m$ with a small charge $q$ is introduced into this region with an initial velocity $\mathbf{v}=\hat{\mathbf{x}} v_{x}+\hat{\mathbf{z}} v_{z}$. Given that $B, m, q, v_{x}$ and $v_{z}$ are all non-zero, which one of the following describes the eventual trajectory of the particle?
(A) Helical motion in the $\hat{\mathbf{z}}$ direction.
(B) Circular motion in the $x y$ plane.
(C) Linear motion in the $\hat{\mathbf{z}}$ direction.
(D) Linear motion in the $\hat{\mathbf{x}}$ direction.
Q. 24 Let the electric field vector of a plane electromagnetic wave propagating in a homogenous medium be expressed as $\mathbf{E}=\hat{\mathbf{x}} E_{x} e^{-j(\omega t-\beta z)}$, where the propagation constant $\beta$ is a function of the angular frequency $\omega$. Assume that $\beta(\omega)$ and $E_{x}$ are known and are real. From the information available, which one of the following CANNOT be determined?
(A) The type of polarization of the wave.
(B) The group velocity of the wave.
(C) The phase velocity of the wave.
(D) The power flux through the $z=0$ plane.
Q. 25 Light from free space is incident at an angle $\theta_{i}$ to the normal of the facet of a step-index large core optical fibre. The core and cladding refractive indices are $n_{1}=1.5$ and $n_{2}=1.4$, respectively.


The maximum value of $\theta_{i}$ (in degrees) for which the incident light will be guided in the core of the fibre is $\qquad$

## Q. 26 - Q. 55 carry two marks each.

Q. 26 The ordinary differential equation

$$
\frac{d x}{d t}=-3 x+2, \text { with } x(0)=1
$$

is to be solved using the forward Euler method. The largest time step that can be used to solve the equation without making the numerical solution unstable is $\qquad$
Q. 27 Suppose C is the closed curve defined as the circle $x^{2}+y^{2}=1$ with C oriented anti-clockwise. The value of $\oint\left(x y^{2} d x+x^{2} y d y\right)$ over the curve C equals $\qquad$
Q. 28 Two random variables $X$ and $Y$ are distributed according to

$$
f_{X, Y}(x, y)= \begin{cases}(x+y), & 0 \leq x \leq 1, \quad 0 \leq y \leq 1 \\ 0, & \text { otherwise }\end{cases}
$$

The probability $P(X+Y \leq 1)$ is $\qquad$
Q. 29

The matrix $A=\left[\begin{array}{cccc}a & 0 & 3 & 7 \\ 2 & 5 & 1 & 3 \\ 0 & 0 & 2 & 4 \\ 0 & 0 & 0 & b\end{array}\right]$ has $\operatorname{det}(A)=100$ and $\operatorname{trace}(A)=14$.
The value of $|a-b|$ is $\qquad$
Q. 30 In the given circuit, each resistor has a value equal to $1 \Omega$.


What is the equivalent resistance across the terminals $a$ and $b$ ?
(A) $1 / 6 \Omega$
(B) $1 / 3 \Omega$
(C) $9 / 20 \Omega$
(D) $8 / 15 \Omega$
Q. 31 In the circuit shown in the figure, the magnitude of the current (in amperes) through $R_{2}$ is $\qquad$

Q. 32 A continuous-time filter with transfer function $H(s)=\frac{2 s+6}{s^{2}+6 s+8}$ is converted to a discretetime filter with transfer function $G(z)=\frac{2 z^{2}-0.5032 z}{z^{2}-0.5032 z+k}$ so that the impulse response of the continuous-time filter, sampled at 2 Hz , is identical at the sampling instants to the impulse response of the discrete time filter. The value of $k$ is $\qquad$
Q. 33 The Discrete Fourier Transform (DFT) of the 4-point sequence
$x[n]=\{x[0], x[1], x[2], x[3]\}=\{3,2,3,4\}$ is
$X[k]=\{X[0], X[1], X[2], X[3]\}=\{12,2 j, 0,-2 j\}$.
If $X_{1}[k]$ is the DFT of the 12-point sequence $x_{1}[n]=\{3,0,0,2,0,0,3,0,0,4,0,0\}$, the value of $\left|\frac{X_{1}[8]}{X_{1}[11]}\right|$ is $\qquad$
Q. 34 The switch S in the circuit shown has been closed for a long time. It is opened at time $t=0$ and remains open after that. Assume that the diode has zero reverse current and zero forward voltage drop.


The steady state magnitude of the capacitor voltage $V_{\mathrm{C}}$ (in volts) is $\qquad$
Q. 35 A voltage $V_{G}$ is applied across a MOS capacitor with metal gate and p-type silicon substrate at $\mathrm{T}=300 \mathrm{~K}$. The inversion carrier density (in number of carriers per unit area) for $V_{G}=0.8 \mathrm{~V}$ is $2 \times 10^{11} \mathrm{~cm}^{-2}$. For $V_{G}=1.3 \mathrm{~V}$, the inversion carrier density is $4 \times 10^{11} \mathrm{~cm}^{-2}$. What is the value of the inversion carrier density for $V_{G}=1.8 \mathrm{~V}$ ?
(A) $4.5 \times 10^{11} \mathrm{~cm}^{-2}$
(B) $6.0 \times 10^{11} \mathrm{~cm}^{-2}$
(C) $7.2 \times 10^{11} \mathrm{~cm}^{-2}$
(D) $8.4 \times 10^{11} \mathrm{~cm}^{-2}$
Q. 36 Consider avalanche breakdown in a silicon $p^{+} n$ junction. The $n$-region is uniformly doped with a donor density $N_{D}$. Assume that breakdown occurs when the magnitude of the electric field at any point in the device becomes equal to the critical field $E_{\text {crit }}$. Assume $E_{\text {crit }}$ to be independent of $N_{D}$. If the built-in voltage of the $p^{+} n$ junction is much smaller than the breakdown voltage, $V_{B R}$, the relationship between $V_{B R}$ and $N_{D}$ is given by
(A) $V_{B R} \times \sqrt{N_{D}}=$ constant
(B) $N_{D} \times \sqrt{V_{B R}}=$ constant
(C) $N_{D} \times V_{B R}=$ constant
(D) $N_{D} / V_{B R}=$ constant
Q. 37 Consider a region of silicon devoid of electrons and holes, with an ionized donor density of $N_{d}^{+}=10^{17} \mathrm{~cm}^{-3}$. The electric field at $x=0$ is $0 \mathrm{~V} / \mathrm{cm}$ and the electric field at $x=L$ is $50 \mathrm{kV} / \mathrm{cm}$ in the positive $x$ direction. Assume that the electric field is zero in the $y$ and $z$ directions at all points.


Given $q=1.6 \times 10^{-19}$ coulomb, $\epsilon_{0}=8.85 \times 10^{-14} \mathrm{~F} / \mathrm{cm}, \epsilon_{r}=11.7$ for silicon, the value of $L$ in nm is $\qquad$
Q. 38 Consider a long-channel NMOS transistor with source and body connected together. Assume that the electron mobility is independent of $V_{G S}$ and $V_{D S}$. Given,
$g_{m}=0.5 \mu \mathrm{~A} / \mathrm{V}$ for $V_{D S}=50 \mathrm{mV}$ and $V_{G S}=2 \mathrm{~V}$,
$g_{d}=8 \mu \mathrm{~A} / \mathrm{V}$ for $V_{G S}=2 \mathrm{~V}$ and $V_{D S}=0 \mathrm{~V}$,
where $g_{m}=\frac{\partial I_{D}}{\partial V_{G S}}$ and $g_{d}=\frac{\partial I_{D}}{\partial V_{D S}}$
The threshold voltage (in volts) of the transistor is $\qquad$
Q. 39 The figure shows a half-wave rectifier with a $475 \mu \mathrm{~F}$ filter capacitor. The load draws a constant current $I_{O}=1 \mathrm{~A}$ from the rectifier. The figure also shows the input voltage $V_{i}$, the output voltage $V_{C}$ and the peak-to-peak voltage ripple $u$ on $V_{C}$. The input voltage $V_{i}$ is a triangle-wave with an amplitude of 10 V and a period of 1 ms .



The value of the ripple $u$ (in volts) is $\qquad$
Q. 40 In the opamp circuit shown, the Zener diodes $Z 1$ and $Z 2$ clamp the output voltage $V_{O}$ to +5 V or -5 V . The switch S is initially closed and is opened at time $t=0$.


The time $t=t_{1}$ (in seconds) at which $V_{O}$ changes state is $\qquad$
Q. 41 An opamp has a finite open loop voltage gain of 100 . Its input offset voltage $\mathrm{V}_{\text {ios }}(=+5 \mathrm{mV})$ is modeled as shown in the circuit below. The amplifier is ideal in all other respects. $V_{\text {input }}$ is 25 mV .


The output voltage (in millivolts) is $\qquad$
Q. 42 An 8 Kbyte ROM with an active low Chip Select input ( $\overline{\mathrm{CS}}$ ) is to be used in an 8085 microprocessor based system. The ROM should occupy the address range 1000 H to 2FFFH. The address lines are designated as $A_{15}$ to $A_{0}$, where $A_{15}$ is the most significant address bit.
Which one of the following logic expressions will generate the correct $\overline{\mathrm{CS}}$ signal for this ROM?
(A) $A_{15}+A_{14}+\left(A_{13} \cdot A_{12}+\overline{A_{13}} \cdot \overline{A_{12}}\right)$
(B) $A_{15} \cdot A_{14} \cdot\left(A_{13}+A_{12}\right)$
(C) $\overline{A_{15}} \cdot \overline{A_{14}} \cdot\left(A_{13} \cdot \overline{A_{12}}+\overline{A_{13}} \cdot A_{12}\right)$
(D) $\overline{A_{15}}+\overline{A_{14}}+A_{13} \cdot A_{12}$
Q. 43 In an N bit flash ADC, the analog voltage is fed simultaneously to $2^{N}-1$ comparators. The output of the comparators is then encoded to a binary format using digital circuits. Assume that the analog voltage source $V_{\text {in }}$ (whose output is being converted to digital format) has a source resistance of $75 \Omega$ as shown in the circuit diagram below and the input capacitance of each comparator is 8 pF . The input must settle to an accuracy of $1 / 2$ LSB even for a full scale input change for proper conversion. Assume that the time taken by the thermometer to binary encoder is negligible.


If the flash ADC has 8 bit resolution, which one of the following alternatives is closest to the maximum sampling rate ?
(A) 1 megasamples per second
(B) 6 megasamples per second
(C) 64 megasamples per second
(D) 256 megasamples per second
Q. 44 The state transition diagram for a finite state machine with states A, B and C, and binary inputs X, Y and Z , is shown in the figure.


Which one of the following statements is correct?
(A) Transitions from State A are ambiguously defined.
(B) Transitions from State B are ambiguously defined.
(C) Transitions from State C are ambiguously defined.
(D) All of the state transitions are defined unambiguously.
Q. 45 In the feedback system shown below $G(s)=\frac{1}{\left(s^{2}+2 s\right)}$.

The step response of the closed-loop system should have minimum settling time and have no overshoot.


The required value of gain $k$ to achieve this is $\qquad$
Q. 46 In the feedback system shown below $G(s)=\frac{1}{(s+1)(s+2)(s+3)}$.


The positive value of $k$ for which the gain margin of the loop is exactly 0 dB and the phase margin of the loop is exactly zero degree is $\qquad$
Q. 47 The asymptotic Bode phase plot of $G(s)=\frac{k}{(s+0.1)(s+10)\left(s+p_{1}\right)}$, with $k$ and $p_{1}$ both positive, is shown below.


The value of $p_{1}$ is $\qquad$
Q. 48 An information source generates a binary sequence $\left\{\alpha_{n}\right\}$. $\alpha_{n}$ can take one of the two possible values -1 and +1 with equal probability and are statistically independent and identically distributed. This sequence is precoded to obtain another sequence $\left\{\beta_{n}\right\}$, as $\beta_{n}=\alpha_{n}+k \alpha_{n-3}$. The sequence $\left\{\beta_{n}\right\}$ is used to modulate a pulse $g(t)$ to generate the baseband signal $X(t)=\sum_{n=-\infty}^{\infty} \beta_{n} g(t-n T)$, where $g(t)= \begin{cases}1, & 0 \leq t \leq T \\ 0, & \text { otherwise } .\end{cases}$ If there is a null at $f=\frac{1}{3 T}$ in the power spectral density of $X(t)$, then $k$ is $\qquad$
Q. 49 An ideal band-pass channel $500 \mathrm{~Hz}-2000 \mathrm{~Hz}$ is deployed for communication. A modem is designed to transmit bits at the rate of 4800 bits/s using 16-QAM. The roll-off factor of a pulse with a raised cosine spectrum that utilizes the entire frequency band is $\qquad$ .
Q. 50 Consider a random process $X(t)=3 V(t)-8$, where $V(t)$ is a zero mean stationary random process with autocorrelation $R_{v}(\tau)=4 e^{-5 \mid \tau \tau}$. The power in $X(t)$ is $\qquad$
Q. 51 A binary communication system makes use of the symbols "zero" and "one". There are channel errors. Consider the following events:

$$
\begin{aligned}
& x_{0}: \text { a "zero" is transmitted } \\
& x_{1}: \text { a "one" is transmitted } \\
& y_{0}: \text { a "zero" is received } \\
& y_{1}: \text { a "one" is received }
\end{aligned}
$$

The following probabilities are given: $P\left(x_{0}\right)=\frac{1}{2}, P\left(y_{0} \mid x_{0}\right)=\frac{3}{4}$, and $P\left(y_{0} \mid x_{1}\right)=\frac{1}{2}$. The information in bits that you obtain when you learn which symbol has been received (while you know that a "zero" has been transmitted) is $\qquad$
Q. 52 The parallel-plate capacitor shown in the figure has movable plates. The capacitor is charged so that the energy stored in it is $E$ when the plate separation is $d$. The capacitor is then isolated electrically and the plates are moved such that the plate separation becomes $2 d$.


At this new plate separation, what is the energy stored in the capacitor, neglecting fringing effects?
(A) $2 E$
(B) $\sqrt{2} E$
(C) $E$
(D) $E / 2$
Q. 53 A lossless microstrip transmission line consists of a trace of width $w$. It is drawn over a practically infinite ground plane and is separated by a dielectric slab of thickness $t$ and relative permittivity $\varepsilon_{r}>1$. The inductance per unit length and the characteristic impedance of this line are $L$ and $Z_{0}$, respectively.


Which one of the following inequalities is always satisfied?
(A) $Z_{0}>\sqrt{\frac{L t}{\varepsilon_{0} \varepsilon_{r} w}}$
(B) $Z_{0}<\sqrt{\frac{L t}{\varepsilon_{0} \varepsilon_{r} w}}$
(C) $Z_{0}>\sqrt{\frac{L w}{\varepsilon_{0} \varepsilon_{r} t}}$
(D) $Z_{0}<\sqrt{\frac{L W}{\varepsilon_{0} \varepsilon_{r} t}}$
Q. 54 A microwave circuit consisting of lossless transmission lines $T_{1}$ and $T_{2}$ is shown in the figure. The plot shows the magnitude of the input reflection coefficient $\Gamma$ as a function of frequency $f$. The phase velocity of the signal in the transmission lines is $2 \times 10^{8} \mathrm{~m} / \mathrm{s}$.



The length $L$ (in meters) of $\mathrm{T}_{2}$ is $\qquad$
Q. 55 A positive charge $q$ is placed at $x=0$ between two infinite metal plates placed at $x=-d$ and at $x=+d$ respectively. The metal plates lie in the $y z$ plane.


The charge is at rest at $t=0$, when a voltage $+V$ is applied to the plate at $-d$ and voltage $-V$ is applied to the plate at $x=+d$. Assume that the quantity of the charge $q$ is small enough that it does not perturb the field set up by the metal plates. The time that the charge $q$ takes to reach the right plate is proportional to
(A) $d / V$
(B) $\sqrt{d} / V$
(C) $d / \sqrt{V}$
(D) $\sqrt{d / V}$

## Q. 1 - Q. 5 carry one mark each.

Q. 1 An apple costs Rs. 10. An onion costs Rs. 8.

Select the most suitable sentence with respect to grammar and usage.
(A) The price of an apple is greater than an onion.
(B) The price of an apple is more than onion.
(C) The price of an apple is greater than that of an onion.
(D) Apples are more costlier than onions.
Q. 2 The Buddha said, "Holding on to anger is like grasping a hot coal with the intent of throwing it at someone else; you are the one who gets burnt."

Select the word below which is closest in meaning to the word underlined above.
(A) burning
(B) igniting
(C) clutching
(D) flinging
Q. $3 \quad \mathbf{M}$ has a son $\mathbf{Q}$ and a daughter $\mathbf{R}$. He has no other children. $\mathbf{E}$ is the mother of $\mathbf{P}$ and daughter-inlaw of $\mathbf{M}$. How is $\mathbf{P}$ related to $\mathbf{M}$ ?
(A) $\mathbf{P}$ is the son-in-law of $\mathbf{M}$.
(B) $\mathbf{P}$ is the grandchild of $\mathbf{M}$.
(C) $\mathbf{P}$ is the daughter-in law of $\mathbf{M}$.
(D) $\mathbf{P}$ is the grandfather of $\mathbf{M}$.
Q. 4 The number that least fits this set: $(324,441,97$ and 64$)$ is $\qquad$ .
(A) 324
(B) 441
(C) 97
(D) 64
Q. 5 It takes 10 s and 15 s , respectively, for two trains travelling at different constant speeds to completely pass a telegraph post. The length of the first train is 120 m and that of the second train is 150 m . The magnitude of the difference in the speeds of the two trains (in $\mathrm{m} / \mathrm{s}$ ) is $\qquad$ .
(A) 2.0
(B) 10.0
(C) 12.0
(D) 22.0

## Q. 6 - Q. 10 carry two marks each.

Q. 6 The velocity V of a vehicle along a straight line is measured in $\mathrm{m} / \mathrm{s}$ and plotted as shown with respect to time in seconds. At the end of the 7 seconds, how much will the odometer reading increase by (in m )?

(A) 0
(B) 3
(C) 4
(D) 5
Q. 7 The overwhelming number of people infected with rabies in India has been flagged by the World Health Organization as a source of concern. It is estimated that inoculating $70 \%$ of pets and stray dogs against rabies can lead to a significant reduction in the number of people infected with rabies.

Which of the following can be logically inferred from the above sentences?
(A) The number of people in India infected with rabies is high.
(B) The number of people in other parts of the world who are infected with rabies is low.
(C) Rabies can be eradicated in India by vaccinating 70\% of stray dogs.
(D) Stray dogs are the main source of rabies worldwide.
Q. 8 A flat is shared by four first year undergraduate students. They agreed to allow the oldest of them to enjoy some extra space in the flat. Manu is two months older than Sravan, who is three months younger than Trideep. Pavan is one month older than Sravan. Who should occupy the extra space in the flat?
(A) Manu
(B) Sravan
(C) Trideep
(D) Pavan
Q. 9 Find the area bounded by the lines $3 x+2 y=14,2 x-3 y=5$ in the first quadrant.
(A) 14.95
(B) 15.25
(C) 15.70
(D) 20.35
Q. 10 A straight line is fit to a data set $(\ln x, y)$. This line intercepts the abscissa at $\ln x=0.1$ and has a slope of -0.02 . What is the value of $y$ at $x=5$ from the fit?
(A) -0.030
(B) -0.014
(C) 0.014
(D) 0.030

## END OF THE QUESTION PAPER

## Q. 1 - Q. 25 carry one mark each.

Q. 1 Consider a $2 \times 2$ square matrix

$$
\mathbf{A}=\left[\begin{array}{ll}
\sigma & x \\
\omega & \sigma
\end{array}\right],
$$

where $x$ is unknown. If the eigenvalues of the matrix $\mathbf{A}$ are $(\sigma+j \omega)$ and $(\sigma-j \omega)$, then $x$ is equal to
(A) $+j \omega$
(B) $-j \omega$
(C) $+\omega$
(D) $-\omega$
Q. 2 For $f(z)=\frac{\sin (z)}{z^{2}}$, the residue of the pole at $z=0$ is $\qquad$
Q. 3 The probability of getting a "head" in a single toss of a biased coin is 0.3 . The coin is tossed repeatedly till a "head" is obtained. If the tosses are independent, then the probability of getting "head" for the first time in the fifth toss is $\qquad$
Q. 4 The integral $\int_{0}^{1} \frac{d x}{\sqrt{(1-x)}}$ is equal to $\qquad$
Q. 5 Consider the first order initial value problem

$$
y^{\prime}=y+2 x-x^{2}, \quad y(0)=1,(0 \leq x<\infty)
$$

with exact solution $y(x)=x^{2}+e^{x}$. For $x=0.1$, the percentage difference between the exact solution and the solution obtained using a single iteration of the second-order Runge-Kutta method with step-size $h=0.1$ is $\qquad$
Q. 6 Consider the signal $x(t)=\cos (6 \pi t)+\sin (8 \pi t)$, where $t$ is in seconds. The Nyquist sampling rate (in samples/second) for the signal $y(t)=x(2 t+5)$ is
(A) 8
(B) 12
(C) 16
(D) 32
Q. 7 If the signal $x(t)=\frac{\sin (t)}{\pi t} * \frac{\sin (t)}{\pi t}$ with $*$ denoting the convolution operation, then $x(t)$ is equal to
(A) $\frac{\sin (t)}{\pi t}$
(B) $\frac{\sin (2 t)}{2 \pi t}$
(C) $\frac{2 \sin (t)}{\pi t}$
(D) $\left(\frac{\sin (t)}{\pi t}\right)^{2}$
Q. $8 \quad$ A discrete-time signal $x[n]=\delta[n-3]+2 \delta[n-5]$ has $z$-transform $X(z)$. If $Y(z)=X(-z)$ is the $z$-transform of another signal $y[n]$, then
(A) $y[n]=x[n]$
(B) $y[n]=x[-n]$
(C) $y[n]=-x[n]$
(D) $y[n]=-x[-n]$
Q. 9 In the RLC circuit shown in the figure, the input voltage is given by

$$
v_{i}(t)=2 \cos (200 t)+4 \sin (500 t) .
$$

The output voltage $v_{o}(t)$ is

(A) $\cos (200 t)+2 \sin (500 t)$
(B) $2 \cos (200 t)+4 \sin (500 t)$
(C) $\sin (200 t)+2 \cos (500 t)$
(D) $2 \sin (200 t)+4 \cos (500 t)$
Q. 10 The I-V characteristics of three types of diodes at the room temperature, made of semiconductors $\mathrm{X}, \mathrm{Y}$ and Z , are shown in the figure. Assume that the diodes are uniformly doped and identical in all respects except their materials. If $\mathrm{E}_{\mathrm{gx}}, \mathrm{E}_{\mathrm{gY}}$ and $\mathrm{E}_{\mathrm{gz}}$ are the band gaps of $\mathrm{X}, \mathrm{Y}$ and Z , respectively, then

(A) $\mathrm{E}_{\mathrm{gX}}>\mathrm{E}_{\mathrm{gY}}>\mathrm{E}_{\mathrm{gz}}$
(B) $\mathrm{E}_{\mathrm{gX}}=\mathrm{E}_{\mathrm{gy}}=\mathrm{E}_{\mathrm{gz}}$
(C) $\mathrm{E}_{\mathrm{gX}}<\mathrm{E}_{\mathrm{gY}}<\mathrm{E}_{\mathrm{gZ}}$
(D) no relationship among these band gaps exists.
Q. 11 The figure shows the band diagram of a Metal Oxide Semiconductor (MOS). The surface region of this MOS is in

(A) inversion
(B) accumulation
(C) depletion
(D) flat band
Q. 12 The figure shows the I-V characteristics of a solar cell illuminated uniformly with solar light of power $100 \mathrm{~mW} / \mathrm{cm}^{2}$. The solar cell has an area of $3 \mathrm{~cm}^{2}$ and a fill factor of 0.7 . The maximum efficiency (in \%) of the device is $\qquad$

Q. 13 The diodes D1 and D2 in the figure are ideal and the capacitors are identical. The product RC is very large compared to the time period of the ac voltage. Assuming that the diodes do not breakdown in the reverse bias, the output voltage $\mathrm{V}_{\mathrm{O}}$ (in volt) at the steady state is $\qquad$

Q. 14 Consider the circuit shown in the figure. Assuming $\mathrm{V}_{\mathrm{BE} 1}=\mathrm{V}_{\mathrm{EB} 2}=0.7$ volt, the value of the dc voltage $\mathrm{V}_{\mathrm{C} 2}$ (in volt) is $\qquad$

Q. 15 In the astable multivibrator circuit shown in the figure, the frequency of oscillation (in kHz ) at the output pin 3 is $\qquad$

Q. 16 In an 8085 microprocessor, the contents of the accumulator and the carry flag are A7 (in hex) and 0, respectively. If the instruction RLC is executed, then the contents of the accumulator (in hex) and the carry flag, respectively, will be
(A) 4 E and 0
(B) 4E and 1
(C) 4 F and 0
(D) 4F and 1
Q. 17 The logic functionality realized by the circuit shown below is

(A) OR
(B) XOR
(C) NAND
(D) AND
Q. 18 The minimum number of 2-input NAND gates required to implement a 2-input XOR gate is
(A) 4
(B) 5
(C) 6
(D) 7
Q. 19 The block diagram of a feedback control system is shown in the figure. The overall closed-loop gain $G$ of the system is

(A) $G=\frac{G_{1} G_{2}}{1+G_{1} H_{1}}$
(B) $G=\frac{G_{1} G_{2}}{1+G_{1} G_{2}+G_{1} H_{1}}$
(C) $G=\frac{G_{1} G_{2}}{1+G_{1} G_{2} H_{1}}$
(D) $G=\frac{G_{1} G_{2}}{1+G_{1} G_{2}+G_{1} G_{2} H_{1}}$
Q. 20 For the unity feedback control system shown in the figure, the open-loop transfer function $G(s)$ is given as

$$
G(s)=\frac{2}{s(s+1)}
$$

The steady state error $e_{s s}$ due to a unit step input is

(A) 0
(B) 0.5
(C) 1.0
(D) $\infty$
Q. 21 For a superheterodyne receiver, the intermediate frequency is 15 MHz and the local oscillator frequency is 3.5 GHz . If the frequency of the received signal is greater than the local oscillator frequency, then the image frequency (in MHz ) is $\qquad$
Q. 22 An analog baseband signal, bandlimited to 100 Hz , is sampled at the Nyquist rate. The samples are quantized into four message symbols that occur independently with probabilities $p_{1}=p_{4}=0.125$ and $p_{2}=p_{3}$. The information rate (bits/sec) of the message source is $\qquad$
Q. 23 A binary baseband digital communication system employs the signal

$$
p(\mathrm{t})= \begin{cases}\frac{1}{\sqrt{\mathrm{~T}_{\mathrm{S}}}}, & 0 \leq \mathrm{t} \leq \mathrm{T}_{\mathrm{S}} \\ 0, & \text { otherwise }\end{cases}
$$

for transmission of bits. The graphical representation of the matched filter output $\mathrm{y}(\mathrm{t})$ for this signal will be
(A)

(B)

(C)

(D)

Q. 24 If a right-handed circularly polarized wave is incident normally on a plane perfect conductor, then the reflected wave will be
(A) right-handed circularly polarized
(B) left-handed circularly polarized
(C) elliptically polarized with a tilt angle of $45^{\circ}$
(D) horizontally polarized
Q. 25 Faraday's law of electromagnetic induction is mathematically described by which one of the following equations?
(A) $\nabla \bullet \vec{B}=0$
(B) $\nabla \bullet \vec{D}=\rho_{V}$
(C) $\nabla \times \vec{E}=-\frac{\partial \vec{B}}{\partial t}$
(D) $\nabla \times \vec{H}=\sigma \vec{E}+\frac{\partial \vec{D}}{\partial t}$

## Q. 26 - Q. 55 carry two marks each.

Q. 26 The particular solution of the initial value problem given below is

$$
\frac{d^{2} y}{d x^{2}}+12 \frac{d y}{d x}+36 y=0 \quad \text { with } \quad y(0)=3 \quad \text { and }\left.\quad \frac{d y}{d x}\right|_{x=0}=-36
$$

(A) $(3-18 x) \mathrm{e}^{-6 x}$
(B) $(3+25 x) \mathrm{e}^{-6 x}$
(C) $(3+20 x) \mathrm{e}^{-6 x}$
(D) $(3-12 x) \mathrm{e}^{-6 x}$
Q. 27 If the vectors $\mathbf{e}_{1}=(1,0,2), \mathbf{e}_{2}=(0,1,0)$ and $\mathbf{e}_{3}=(-2,0,1)$ form an orthogonal basis of the threedimensional real space $\mathbb{R}^{3}$, then the vector $\mathbf{u}=(4,3,-3) \in \mathbb{R}^{3}$ can be expressed as
(A) $\mathbf{u}=-\frac{2}{5} \mathbf{e}_{1}-3 \mathbf{e}_{2}-\frac{11}{5} \mathbf{e}_{3}$
(B) $\mathbf{u}=-\frac{2}{5} \mathbf{e}_{1}-3 \mathbf{e}_{2}+\frac{11}{5} \mathbf{e}_{3}$
(C) $\mathbf{u}=-\frac{2}{5} \mathbf{e}_{1}+3 \mathbf{e}_{2}+\frac{11}{5} \mathbf{e}_{3}$
(D) $\mathbf{u}=-\frac{2}{5} \mathbf{e}_{1}+3 \mathbf{e}_{2}-\frac{11}{5} \mathbf{e}_{3}$
Q. 28 A triangle in the $x y$-plane is bounded by the straight lines $2 x=3 y, y=0$ and $x=3$. The volume above the triangle and under the plane $x+y+z=6$ is $\qquad$
Q. 29 The values of the integral $\frac{1}{2 \pi j} \oint_{c} \frac{e^{z}}{z-2} d z$ along a closed contour $c$ in anti-clockwise direction for
(i) the point $z_{0}=2$ inside the contour $c$, and
(ii) the point $z_{0}=2$ outside the contour $c$, respectively, are
(A) (i) 2.72,
(ii) 0
(B) (i) 7.39 ,
(ii) 0
(C) (i) 0 ,
(ii) 2.72
(D) (i) 0 ,
(ii) 7.39
Q. 30 A signal $2 \cos \left(\frac{2 \pi}{3} t\right)-\cos (\pi t)$ is the input to an LTI system with the transfer function

$$
H(s)=e^{s}+e^{-s} .
$$

If $C_{k}$ denotes the $k^{\text {th }}$ coefficient in the exponential Fourier series of the output signal, then $C_{3}$ is equal to
(A) 0
(B) 1
(C) 2
(D) 3
Q. 31 The ROC (region of convergence) of the $z$-transform of a discrete-time signal is represented by the shaded region in the $z$-plane. If the signal $x[n]=(2.0)^{|n|},-\infty<n<+\infty$, then the ROC of its $z$-transform is represented by
(A)

(B)

(C)

(D)

Q. 32 Assume that the circuit in the figure has reached the steady state before time $t=0$ when the $3 \Omega$ resistor suddenly burns out, resulting in an open circuit. The current $i(t)$ (in ampere) at $t=0^{+}$is
$\qquad$

Q. 33 In the figure shown, the current $i$ (in ampere) is $\qquad$

Q. 34

The z-parameter matrix $\left[\begin{array}{ll}z_{11} & z_{12} \\ z_{21} & z_{22}\end{array}\right]$ for the two-port network shown is

(A) $\left[\begin{array}{cc}2 & -2 \\ -2 & 2\end{array}\right]$
(B) $\left[\begin{array}{ll}2 & 2 \\ 2 & 2\end{array}\right]$
(C) $\left[\begin{array}{cc}9 & -3 \\ 6 & 9\end{array}\right]$
(D) $\left[\begin{array}{ll}9 & 3 \\ 6 & 9\end{array}\right]$
Q. 35 A continuous-time speech signal $x_{a}(t)$ is sampled at a rate of 8 kHz and the samples are subsequently grouped in blocks, each of size $N$. The DFT of each block is to be computed in real time using the radix-2 decimation-in-frequency FFT algorithm. If the processor performs all operations sequentially, and takes $20 \mu \mathrm{~s}$ for computing each complex multiplication (including multiplications by 1 and -1 ) and the time required for addition/subtraction is negligible, then the maximum value of $N$ is $\qquad$
Q. 36 The direct form structure of an FIR (finite impulse response) filter is shown in the figure.


The filter can be used to approximate a
(A) low-pass filter
(B) high-pass filter
(C) band-pass filter
(D) band-stop filter
Q. 37 The injected excess electron concentration profile in the base region of an npn BJT, biased in the active region, is linear, as shown in the figure. If the area of the emitter-base junction is $0.001 \mathrm{~cm}^{2}$, $\mu_{\mathrm{n}}=800 \mathrm{~cm}^{2} /(\mathrm{V}-\mathrm{s})$ in the base region and depletion layer widths are negligible, then the collector current $\mathrm{I}_{\mathrm{C}}$ (in mA ) at room temperature is $\qquad$
(Given: thermal voltage $\mathrm{V}_{\mathrm{T}}=26 \mathrm{mV}$ at room temperature, electronic charge $q=1.6 \times 10^{-19} \mathrm{C}$ )

Q. 38 Figures I and II show two MOS capacitors of unit area. The capacitor in Figure I has insulator materials $X$ (of thickness $\mathrm{t}_{1}=1 \mathrm{~nm}$ and dielectric constant $\varepsilon_{1}=4$ ) and Y (of thickness $\mathrm{t}_{2}=3 \mathrm{~nm}$ and dielectric constant $\varepsilon_{2}=20$ ). The capacitor in Figure II has only insulator material $X$ of thickness $\mathrm{t}_{\mathrm{Eq}}$. If the capacitors are of equal capacitance, then the value of $\mathrm{t}_{\mathrm{Eq}}(\mathrm{in} \mathrm{nm})$ is $\qquad$


Figure II
Q. 39 The I-V characteristics of the zener diodes D1 and D2 are shown in Figure I. These diodes are used in the circuit given in Figure II. If the supply voltage is varied from 0 to 100 V , then breakdown occurs in

(A) D1 only
(B) D2 only
(C) both D1and D2
(D) none of D1 and D2
Q. 40 For the circuit shown in the figure, $R_{1}=R_{2}=R_{3}=1 \Omega, L=1 \mu \mathrm{H}$ and $C=1 \mu \mathrm{~F}$. If the input $\mathrm{V}_{\text {in }}=\cos \left(10^{6} t\right)$, then the overall voltage gain $\left(\mathrm{V}_{\text {out }} / \mathrm{V}_{\text {in }}\right)$ of the circuit is $\qquad$

Q. 41 In the circuit shown in the figure, the channel length modulation of all transistors is non-zero $(\lambda \neq 0)$. Also, all transistors operate in saturation and have negligible body effect. The ac small signal voltage gain $\left(\mathrm{V}_{o} / \mathrm{V}_{\text {in }}\right)$ of the circuit is

(A) $-g_{m 1}\left(r_{o 1}\left\|r_{o 2}\right\| r_{o 3}\right)$
(B) $-g_{m 1}\left(r_{o 1}\left\|\frac{1}{g_{m 3}}\right\| r_{o 3}\right)$
(C) $-g_{m 1}\left(r_{o 1}\left\|\left(\frac{1}{g_{m 2}} \| r_{o 2}\right)\right\| r_{o 3}\right)$
(D) $-g_{m 1}\left(r_{o 1}\left\|\left(\frac{1}{g_{m 3}} \| r_{o 3}\right)\right\| r_{o 2}\right)$
Q. 42 In the circuit shown in the figure, transistor M1 is in saturation and has transconductance $\mathrm{g}_{\mathrm{m}}=0.01$ siemens. Ignoring internal parasitic capacitances and assuming the channel length modulation $\lambda$ to be zero, the small signal input pole frequency (in kHz ) is $\qquad$

Q. 43 Following is the K-map of a Boolean function of five variables $\mathrm{P}, \mathrm{Q}, \mathrm{R}, \mathrm{S}$ and X . The minimum sum-of-product (SOP) expression for the function is


(A) $\overline{\mathrm{P}} \overline{\mathrm{Q}} \mathrm{S} \overline{\mathrm{X}}+\mathrm{P} \overline{\mathrm{Q} S} \overline{\mathrm{X}}+\mathrm{Q} \overline{\mathrm{R}} \overline{\mathrm{S}} \mathrm{X}+\mathrm{QR} \overline{\mathrm{S}} \mathrm{X}$
(B) $\overline{\mathrm{Q}} \mathrm{S} \overline{\mathrm{X}}+\mathrm{Q} \overline{\mathrm{S}} \mathrm{X}$
(C) $\overline{\mathrm{Q}} \mathrm{S} X+\mathrm{Q} \overline{\mathrm{S}} \overline{\mathrm{X}}$
(D) $\overline{\mathrm{Q}} \mathrm{S}+\mathrm{Q} \overline{\mathrm{S}}$
Q. 44 For the circuit shown in the figure, the delays of NOR gates, multiplexers and inverters are 2 ns , 1.5 ns and 1 ns , respectively. If all the inputs $P, Q, R, S$ and $T$ are applied at the same time instant, the maximum propagation delay (in ns) of the circuit is $\qquad$

Q. 45 For the circuit shown in the figure, the delay of the bubbled NAND gate is 2 ns and that of the counter is assumed to be zero.


If the clock (Clk) frequency is 1 GHz , then the counter behaves as a
(A) mod-5 counter
(B) mod-6 counter
(C) mod-7 counter
(D) mod-8 counter
Q. 46 The first two rows in the Routh table for the characteristic equation of a certain closed-loop control system are given as

| $s^{3}$ | 1 | $(2 K+3)$ |
| :---: | :---: | :---: |
| $s^{2}$ | $2 K$ | 4 |

The range of $K$ for which the system is stable is
(A) $-2.0<K<0.5$
(B) $0<K<0.5$
(C) $0<K<\infty$
(D) $0.5<K<\infty$
Q. 47 A second-order linear time-invariant system is described by the following state equations

$$
\begin{gathered}
\frac{d}{d t} x_{1}(t)+2 x_{1}(t)=3 u(t) \\
\frac{d}{d t} x_{2}(t)+x_{2}(t)=u(t)
\end{gathered}
$$

where $x_{1}(t)$ and $x_{2}(t)$ are the two state variables and $u(t)$ denotes the input. If the output $c(t)=x_{1}(t)$, then the system is
(A) controllable but not observable
(B) observable but not controllable
(C) both controllable and observable
(D) neither controllable nor observable
Q. 48 The forward-path transfer function and the feedback-path transfer function of a single loop negative feedback control system are given as

$$
G(s)=\frac{K(s+2)}{s^{2}+2 s+2} \quad \text { and } \quad H(s)=1
$$

respectively. If the variable parameter $K$ is real positive, then the location of the breakaway point on the root locus diagram of the system is $\qquad$
Q. 49 A wide sense stationary random process $X(t)$ passes through the LTI system shown in the figure. If the autocorrelation function of $X(t)$ is $R_{X}(\tau)$, then the autocorrelation function $R_{Y}(\tau)$ of the output $Y(t)$ is equal to

(A) $2 R_{X}(\tau)+R_{X}\left(\tau-T_{0}\right)+R_{X}\left(\tau+T_{0}\right)$
(B) $2 R_{X}(\tau)-R_{X}\left(\tau-T_{0}\right)-R_{X}\left(\tau+T_{0}\right)$
(C) $2 R_{X}(\tau)+2 R_{X}\left(\tau-2 T_{0}\right)$
(D) $2 R_{X}(\tau)-2 R_{X}\left(\tau-2 T_{0}\right)$
Q. 50 A voice-grade AWGN (additive white Gaussian noise) telephone channel has a bandwidth of 4.0 kHz and two-sided noise power spectral density $\frac{\eta}{2}=2.5 \times 10^{-5} \mathrm{Watt}$ per Hz . If information at the rate of 52 kbps is to be transmitted over this channel with arbitrarily small bit error rate, then the minimum bit-energy $E_{b}$ (in $\mathrm{mJ} /$ bit) necessary is $\qquad$
Q. 51 The bit error probability of a memoryless binary symmetric channel is $10^{-5}$. If $10^{5}$ bits are sent over this channel, then the probability that not more than one bit will be in error is $\qquad$
Q. 52 Consider an air-filled rectangular waveguide with dimensions $a=2.286 \mathrm{~cm}$ and $b=1.016 \mathrm{~cm}$. At 10 GHz operating frequency, the value of the propagation constant (per meter) of the corresponding propagating mode is $\qquad$
Q. 53 Consider an air-filled rectangular waveguide with dimensions $a=2.286 \mathrm{~cm}$ and $b=1.016 \mathrm{~cm}$. The increasing order of the cut-off frequencies for different modes is
(A) $\mathrm{TE}_{01}<\mathrm{TE}_{10}<\mathrm{TE}_{11}<\mathrm{TE}_{20}$
(B) $\mathrm{TE}_{20}<\mathrm{TE}_{11}<\mathrm{TE}_{10}<\mathrm{TE}_{01}$
(C) $\mathrm{TE}_{10}<\mathrm{TE}_{20}<\mathrm{TE}_{01}<\mathrm{TE}_{11}$
(D) $\mathrm{TE}_{10}<\mathrm{TE}_{11}<\mathrm{TE}_{20}<\mathrm{TE}_{01}$
Q. 54 A radar operating at 5 GHz uses a common antenna for transmission and reception. The antenna has a gain of 150 and is aligned for maximum directional radiation and reception to a target 1 km away having radar cross-section of $3 \mathrm{~m}^{2}$. If it transmits 100 kW , then the received power (in $\mu \mathrm{W}$ ) is
Q. 55 Consider the charge profile shown in the figure. The resultant potential distribution is best described by

(A)

(B)

(C)

(D)


